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## Fluctuation Analysis of Solar Radio Bursts Associated with Geoeffective X-Class Flares

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**Abstract.** *High temporal resolution solar observations in the decimetric range (1–3 GHz) can provide additional information on solar active regions dynamics and thus contribute to better understanding of solar geoeffective events as flares and coronal mass ejections. The June 06, 2000 flares are a set of remarkable geoeffective eruptive phenomena observed as Solar Radio Bursts (SRB) by means of the 3 GHz Ondrejov Observatory radiometer. We have selected and analyzed, applying Detrended Fluctuation Analysis (DFA), three decimetric bursts associated to X1.1, X1.2 and X2.3 flare-classes, respectively. The association with geomagnetic activity is also reported. DFA method is performed in the framework of a radio burst automatic monitoring system. Our results may characterize the SRB evolution, computing the DFA scaling exponent, scanning the SRB time series by a short windowing before the extreme event. For the first time, the importance of DFA in the context of SRB monitoring analysis is presented.*

**Resumo.** *Observações de alta resolução temporal na faixa decimétrica (1–3GHz) podem fornecer informações adicionais sobre a dinâmica das regiões solares ativas, contribuindo para o melhor entendimento de eventos geofetivos como explosões solares (flares) e ejeções de massa coronal. As explosões solares ocorridas em 06 de Junho de 2000 formam um conjunto de fenômenos eruptivos geofetivos – Solar Radio Bursts (SRB) – observados através do*

*radiômetro de 3GHz do Observatório de Ondrejov. Neste artigo selecionamos e analisamos, aplicando a técnica Detrended Fluctuation Analysis (DFA), três explosões decimétricas associadas às classes X1.1, X1.2 e X2.3, respectivamente. A associação com a atividade geomagnética também é discutida. O método DFA é executado em um sistema de monitoramento automático de explosões de rádio. Os resultados podem caracterizar a evolução do SRB através do cálculo do expoente de escala DFA, percorrendo a série temporal SRB através de um janelamento curto antes do evento extremo. Pela primeira vez, a importância do DFA no contexto da análise para monitoramento é apresentada.*

**Palavras-chave:** *decimetric solar radio bursts, solar flares, detrended fluctuation analysis, computational data analysis, space weather.*

## 1. Introduction

Solar space weather events like coronal mass ejections and solar flares are usually accompanied by solar radio bursts, which can be used for a low-cost real-time space weather monitoring [Lobzin et al. 2009]. However, most of the solar radio flare signals are characterized by complex variability patterns including both non-stationarities and nonlinearities. In fact, radio emission from solar active region electron beams can provide information about the nonlinear electron acceleration/injection processes and the properties of the complex ambient coronal structures [Nindos et al. 2008]. In particular, solar radio emissions in the decimetric frequency range (above 1 GHz) are very rich in temporal and spectral fine structures due to nonlinear processes occurring in the magnetic structures on the corresponding active regions [Aschwanden et al. 2001]. The importance of this decimetric solar flare scenario has been investigated, for example, from nonlinear analysis of decimetric bursts at 3 GHz observed during the June 6, 2000 flare [Rosa et al. 2008]. It was found that the 3 GHz radio burst power spectrum exhibits a power-law which is an evidence of stochastic intermittency due to a self-affine dynamics as found in the MHD turbulence theory. Intermittent energetic process implies that the fluctuations are multi-scaling correlated as predicted in the models for multi-loop interactions [Tajima et al. 1987].

A common practice to characterize decimetric solar radio bursts signals is to record the digital dynamical spectra, extract sequences of single frequency events with limited discrete length (presented as a SFU time series) and to determine quantitative characteristics on the basis of these observations. From a solar radio flare monitoring perspective, the basic strategy is to determine appropriate characteristics of the signal that could be preserved in short temporal moving windowing used to scanning the whole data in a real time procedure providing an radio burst automatic monitoring system (RBAMS). Nowadays, decimetric solar bursts are observed with time resolution ranging from  $10^{-1}$  s to  $10^{-3}$  s. Solar radio flare signals are events ranging from 1 to 10 minutes long (including the pre and post-flare typical intervals), so that a typical decimetric solar burst time series is composed by  $N$  measures ranging from the order of  $10^3$  to  $10^4$  measurement points. As power spectra index (from a  $1/f^\beta$  power-laws), obtained from Fast Fourier Transform (FFT) of the signal auto-correlation function are robust only for  $N \gg 10^3$ , it fails in such monitoring characterization because of relatively short data records for decimetric solar radio bursts which contain stochastic components and non-stationarities.

In this paper it is shown that typical decimetric bursts frequency estimates, obtained from their Fourier-based spectral peaks, are affected by the window length and phase of signal component, thus presenting a large variance and low performance as a candidate measurement for decimetric solar RBAMS. Alternatively, it is shown that the method of *detrended fluctuation analysis* (DFA) [Peng et al. 1994] provides more robust measurements for monitoring solar decimetric bursts.

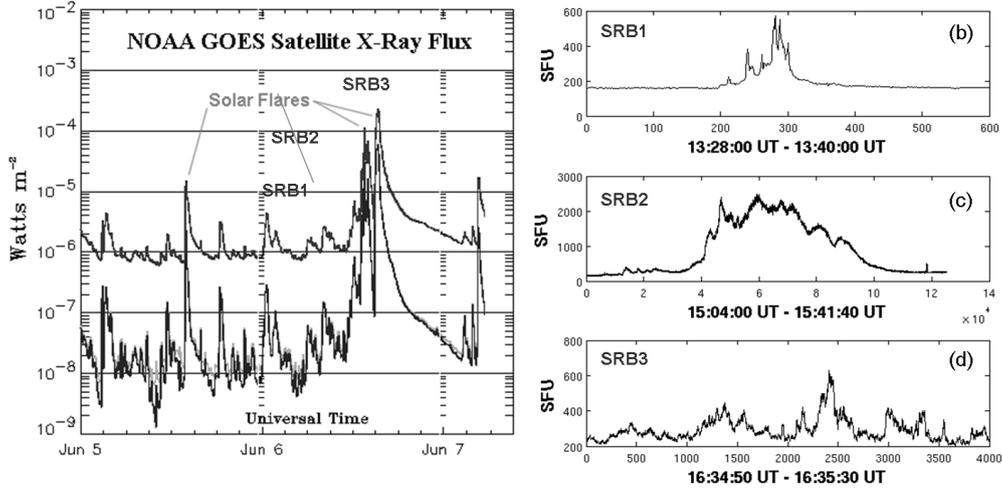
## 2. Solar Radio Burst Data

The June 6, solar filament eruption was accompanied by intense solar flares. A type II radio burst and powerful series of solar eruptions including a full-halo coronal mass ejection (CME) were reported in association with this event (Solar Flare NOAA Report). The June 6, 2000 flares, classified as X1.1, X1.2 and X2.3, respectively, were observed during 13:36–17:00 UT in the active region NOAA AR 9026 (N21, E23). Images of the two main flares X1.2 and X2.3 were observed by the EIT/SOHO and SXT/Yohkoh instruments [Rosa et al. 2005]. The CME activity, associated with the flares in AR 9026, started to increase 17:30 UT reaching its maximum at 19:42 UT. Geomagnetic activity increased on June 8 to major geomagnetic storm conditions, especially at higher latitudes. The maximum intensity for Kyoto University’s real-time Dst index (-90 nT) was recorded at 15:30 UT June 8.

**Tabela 1. The basic characteristics of the June 6, 2000 SRBs observed at 3 GHz.**

Event	SRB1	SRB2	SRB3
$\tau$ (s)	1.2	0.02	0.01
$t_0$ (UT)	13:28:00	15:04:00	16:34:50
$\Delta t_d(N)$	12 min (600)	$\approx 42$ min ( $125 \times 10^3$ )	40 s (4000)
$\Delta t_w(N_w)$	1.2 min (60)	4.2 min (12.500)	4 s (400)
Class Flare (UT)	X1.1 (13:36:00)	X1.2 (15:36:00)	X2.3 (16:35:22)
$\Delta t_{bF}$	8 min.	32 min	32 s
$\Delta t_{bCME}$	6h14min	4h38min	3h08min

Figure 1a shows the NOAA GOES 8 satellite X-ray flux (from channels: 0.5-4.0 A signal under 1.0-8.0 A signal). Three respective SRB were observed employing the Ondrejov 3 GHz radio-spectrograph with time resolution of 0.01 s [Jiricka et al. 1993]. The SRB1 was recorded with lower time resolution,  $\tau = 1.2$  s, from starting time  $t_0 = 13 : 28 : 00$  UT to  $13 : 40 : 00$  UT representing a time series composed of  $N = 600$  digital measurements. The SRB1 duration  $\Delta t_d$  was of 12 minutes. The SRB2 was recorded with higher time resolution,  $\tau = 0.02$  s, from starting time  $t_0 = 15 : 04 : 00$  UT to  $15 : 41 : 40$  UT, representing a time series composed of  $N = 125 \times 10^3$  digital measurements with duration  $\Delta t_d = 42$  minutes. The SRB3 was recorded with the highest time resolution,  $\tau = 0.01$  s, from starting time  $t_0 = 16 : 34 : 50$  UT to  $16 : 35 : 30$  UT, representing a time series composed of  $N = 4000$  digital measurements (then, duration  $\Delta t_d = 40$  seconds). The basic characteristics of the selected SRB are summarized in Table 1, where the time interval before the respective flares and CME peak are reported as  $\Delta t_{bF}$  (column 7th) and  $\Delta t_{bCME}$  (column 8th), respectively. In Table 1 are shown also the windowing intervals  $\Delta t_w(N_w)$  ( $\Delta t_w$  is the time-lag while  $N_w$  is the correspondent number of samples) which will be considered in our DFA analysis in Section 4.1.



**Figure 1. (a) Solar Flares and SRB identification on the X-ray flux in the 1.0 - 8.0 Angstrom band as measured by the NOAA GOES-8 satellite, (b) SRB1, (c) SRB2 and (d) SRB3.**

### 3. Detrended Fluctuation Analysis Method

Detrended Fluctuation Analysis (DFA) measures scaling exponents from non-stationary time series for determining the statistical self-affinity of an underlying dynamical nonlinear process. It is useful for characterizing temporal patterns that appear to be due to long-range memory stochastic processes. DFA has been used in several non-stationary time series analysis from biological and physiological data to finance and space physics signals [Bunde et al. 2000, Buldyrev et al. 1995, Bai and Zhu 2010, Alvarez-Ramirez et al. 2009, Moret et al. 2003].

#### 3.1. DFA algorithm

Detrending methods for fluctuation analysis have been recently proposed and applied for detection of persistent correlations in non-stationary time series analysis [Bashan et al. 2008]. The DFA algorithm considered in our approach, introduced by [Peng et al. 1994], is composed of six computational operations starting on a discrete time series of amplitudes  $\{A_i\}$ :

- *Discrete Integration*: Calculate the cumulative representation of  $\{A_i\}$  as

$$C(k) = \sum_{i=1}^k (A_i - \langle A \rangle), \quad (k = 1, 2, \dots, N) \quad (1)$$

where  $\langle A \rangle = \sum_{i=1}^N A_i / N$  is the average of  $\{A_i\}$ .

- *Windowing*: Using an arbitrary local window of length  $n$ , divide  $C(k)$  into non-overlapping  $N_n = \text{int}(N/n)$  sub-interval  $c_j$  ( $j = 1, 2, \dots, N_n$ ). Note that each sub-interval  $c_j$  has length  $n$  and  $N$  may not be the integer multiple of  $n$ . Then, the series  $C(k)$  is divided once more from the opposite side to make sure all points are addressed, performing at the end of this operation  $2N_n$  sub-intervals.

- **Fitting:** Get, in each sub-interval, the least-square fits as follows:

$$p_j^m(k) = b_{j_0} + b_{j_1}k + \dots + b_{j_{m-1}}k^{m-1} + b_{j_m}k^m, \quad m = 1, 2, \dots \quad (2)$$

where  $m$  is interpreted as the *order of the detrended trend*, denoted here as  $DFA^m$ .

- **Variance:** Compute the cumulative deviation series in every sub-interval, where the trend has been subtracted:  $C_j(k) = C(k) - p_j^m(k)$ . Then, calculate the variance of the  $2N_n$  sub-intervals:

$$F^2(j, n) = \langle C_j^2(i) \rangle = \frac{1}{n} \sum_{i=1}^n [C((j-1)n + i) - p_j^m(i)]^2 \quad (3)$$

for  $j = 1, 2, \dots, N_n$ , and

$$F^2(j, n) = \langle C_j^2(i) \rangle = \frac{1}{n} \sum_{i=1}^n [C(N - (j - N_n)n + i) - p_j^m(i)]^2 \quad (4)$$

for  $j = N_n + 1, N_n + 2, \dots, 2N_n$ .

- **Fluctuation:** Calculate the average of all the variances and the square root to get the fluctuation function of DFA  $F(n)$ :

$$F(n) = \left[ \frac{1}{2N_n} \sum_{j=1}^{2N_n} F^2(j, n) \right]^{1/2}. \quad (5)$$

- **Scaling Exponent:** Perform again, recursively, computation from windowing to calculation of corresponding  $F(n)$  with different  $n$  ( $[N/4] > n \geq 2m + 2$ ) box lengths. In general, in the presence of fluctuations in the form of power law:  $F(n) = Kn^\alpha$ ,  $F(n)$  increases linearly with increasing  $n$ . Then, using the linear least-square regression on the double log plot  $\log F(n) = \log K + \alpha \log n$  one can get the slope  $\alpha$ , which is the scaling exponent of the DFA method.

### 3.2. PSD and DFA

If  $A(t_k)$  is the  $k$ -th value of a time series composed by  $N$  discrete samples with time resolution  $\tau$ , its energy is given by  $E(k) = \sum_0^{N-1} |A(t_k)|^2 \tau$  (for stationary stochastic process of infinite duration, energy is usually infinite) and power of the signal is defined as  $P(k) = E(k)/N\tau$ . Note that the units of  $P$  is the square of the units of the time series and for zero-mean time series the power  $P$  is equal to the variance of  $\{A(t_k)\}$  with  $i = 1, \dots, N$ . Then, the distribution of  $P$  (or variance) of a time series with frequency  $1/T$  (in Hertz, with  $T = \tau + \Delta t$ ) is the so-called Power Spectral Density (PSD) [Kay and Marple 2005]. In practical terms, admitting all possible frequencies from all possible scales  $\Delta t$ , PSD is the squared modulus of the Fourier transform of the rescaled time series and can be estimated based on the direct computation through FFT. In our analysis unit of PSD is  $(s.f.u)^2/Hz$ .

The correlation function  $C(\Delta t)$  decays with an exponent  $C(\Delta t) \approx (\Delta t)^{-\gamma}$  and the PSD decays as  $P(f) \approx (f)^{-\beta}$ , where  $f = 1/\Delta t$ . Thus, the slope of the power spectrum  $\beta$  is usually used to characterize different stochastic processes which are responsible for the autocorrelation range in a given time series. Based on the Wiener-Khinchin theorem [Kay and Marple 2005], it is possible to show that the two exponents  $\beta$  (from PSD) and

$\alpha$  (from DFA) are related by  $\beta = 2\alpha - 1$ . For fractional Brownian motion (a cumulative sum of fractional Gaussian noise) we have  $1 \leq \beta \leq 3$ , and then  $1 \leq \alpha \leq 2$ . The diagnostic potential of PSD and DFA methods is tested on a sub-set of Brownian noise time series. The canonical Brownian noise (fBm) proxy time series was generated from the stochastic system as given by [Osborne and Provenzale 1989] (see [Rosa et al. 2008] for more technical details). A typical canonical Brownian noise, as shown in Figure 2a, can be characterized by  $\beta \approx 2$  and  $\alpha \approx 1.5$ . The fBm data was originally generated having  $2 \times 10^4$  samples (Figure 2a). This signal was sequentially splitted into 5 sub-series containing  $10^4$ ,  $5 \times 10^3$ ,  $10^3$ ,  $5 \times 10^2$ , and 50 samples. Without loss of generality are shown in Figures 2b and 2c the PSD and DFA for the original  $2 \times 10^4$  series and for the sub-set containing the shortest number of samples ( $N = 50$ ). Figures 2b and 2c show that values of  $\beta$  are much less robust than values of  $\alpha$  for short time series with  $N \ll 10^4$ . Figure 2d shows, in a double log plot, both the behaviors of  $\beta$  and  $\alpha$  versus the sub-series size. While the maximum deviation of  $\alpha$  from the expected value is around 8%, the same deviation for  $\beta$  is more than 30%. Then, the use of PSD fails for SRB monitoring because of relatively short data records (as SRB 1 and SRB 3). Figure 2d shows that, for short time series, DFA can detect the correlation length more accurately than the PSD scaling exponent. Our results show that DFA method is especially useful for short records of stochastic and nonlinear processes.

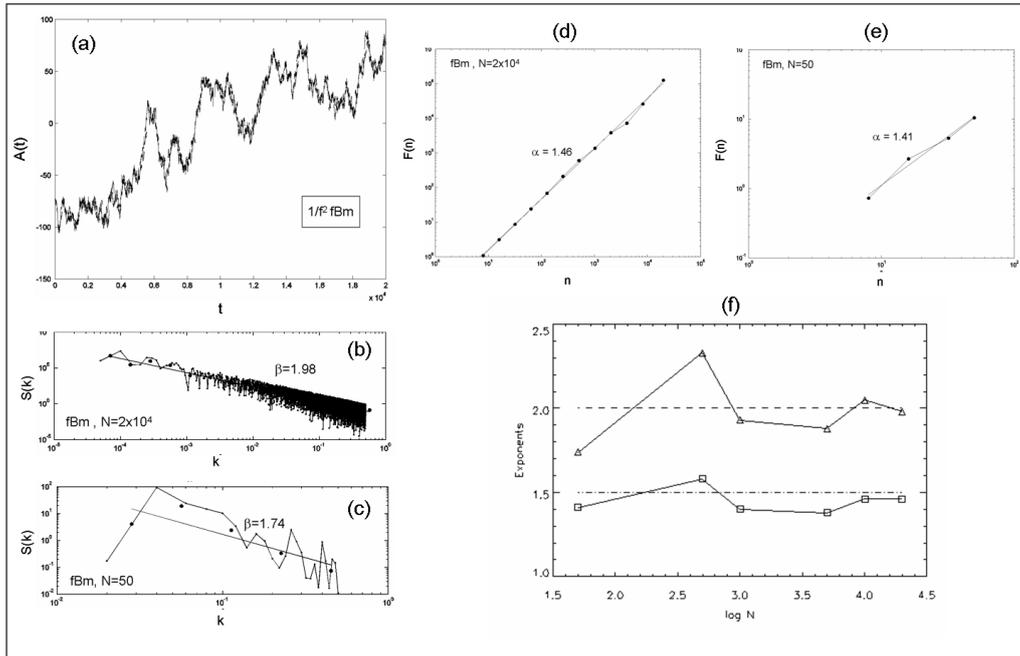
Other methods have been explored to analyze time profiles of solar radio burst – e.g. [Watari 1996] and [Zaitsev et al. 2003]. Even though these methods apprehend some important statistical or geometrical measurement from the data, they present, as PSD, a high bias when it is computed on short time series. It is worthy of note that short time series appear in our context due to the monitoring strategy, which is based on a possible real-time analysis application. The windowing in our approach mimics the real-time analysis in a real monitoring situation. Using fractal dimensions, for example, is out of question for monitoring purposes. The computation of fractal and/or correlation dimensions from 1D time series requires the high computational cost of phase space reconstruction technique (even for box-counting algorithm), whose first condition is to have stationary and long time series ( $\gg 10^3$  points) [Rempel et al. 2004]. The data for the current monitoring analysis are non-stationary (due to turbulent process) and short (due to the monitoring window).

## 4. Analysis of 3 GHz SRB

### 4.1. Global scaling exponents

With the DFA method, we analyze the fluctuations of each 3 GHz SRB. From Figures 3a, 3b and 3c, it is shown that  $1 < \alpha < 2$  characterizes long-range correlations, non-stationary, multi-fractal random walk like and unbounded free-scaling process as predicted from the inhomogeneous multi-looping interaction on the solar active regions. However, the long-range characteristic implies, in the practical sense of using  $\alpha$  as a monitoring measurement, that all the SRB can be analyzed locally for monitoring purposes.

Next we focus on the monitoring local analysis of each burst taking into consideration the time windowing before the peak of each correspondent flare, as shown in figures 3a, 3b and 3c.



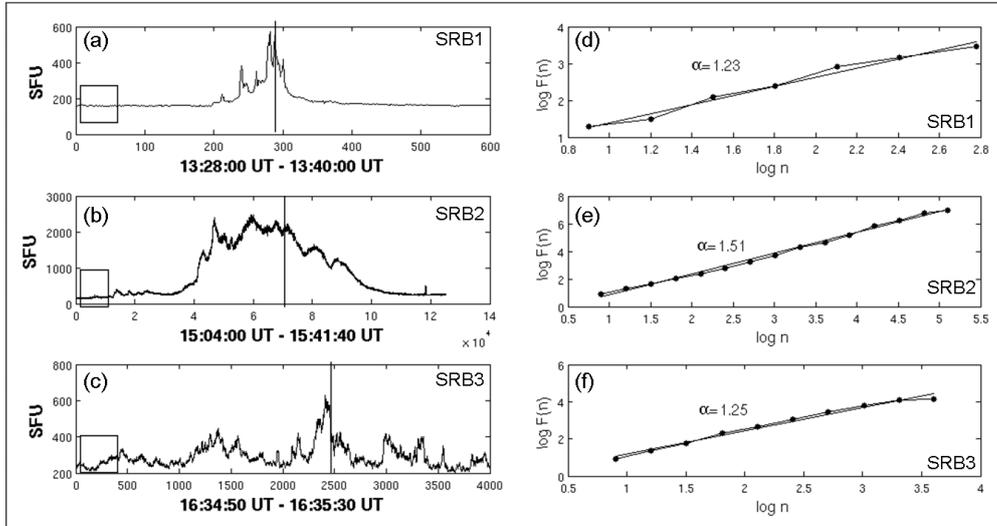
**Figure 2.** (a) fBm noise and their respective PSD (b and c) and DFA (d and e) output. The stability of both scaling exponents are shown in (f),  $\Delta\beta$  is the superior curve around the expected value  $\beta = 2$ .

## 4.2. Local scaling exponents

The size ( $N$ ) of each observed SRB allows us to choose the minimal window length as 10% of  $N$  (see small boxes in Figure 3 a, b and c), providing a minimal set of windows from where a minimal set of DFA scaling exponents, before the related main flare peak (indicated by the vertical lines on the burst profiles of Figure 3), are obtained ( $\approx 10$ ). Comparing, in Figure 4, the scaling exponent evolution before the correspondent flare, one can see that, despite the nonlinear behavior of  $\alpha$ , the obtained limit value when the flare starts are the maximum values for  $\alpha$ . Such behavior of  $\alpha$  from DFA analysis of SRB can be useful in a framework of operational data analysis providing monitoring, alerts and forecasts of solar flares and, possibly, of geomagnetic activity.

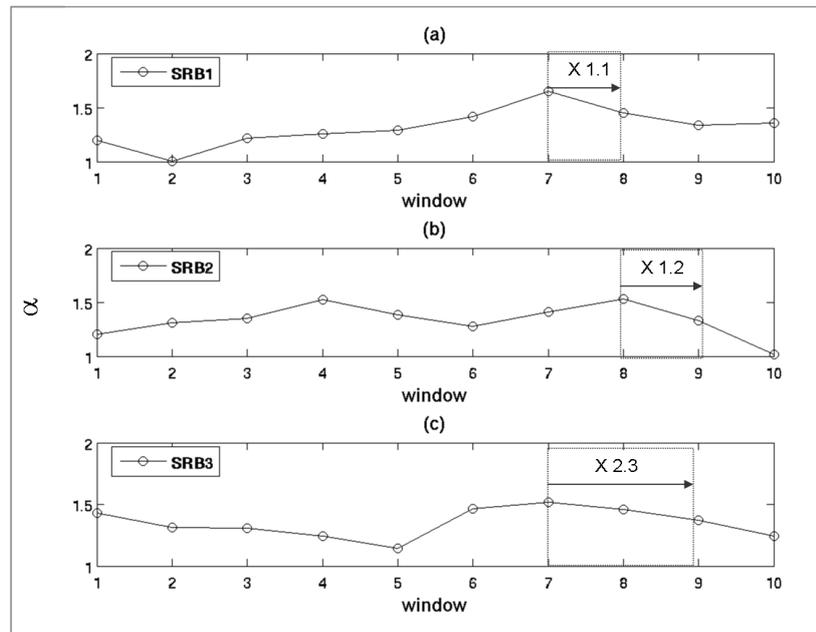
## 5. Concluding Remarks

Stochastic intermittent fluctuations are characterized by time series that display multi-scaling, irregular and quasi-regular amplitudes. Usually, intermittency is a characteristic of the underlying dynamics and it is difficult to quantify, since it appears in many variability patterns. Recently, it was shown that decimetric solar bursts observed at 3 GHz mutual interacting solar loop with nonlinear oscillations require models considering both anisotropy and intermittency. Thus, in the phenomenological analysis of the 3 GHz solar flare considering the scenario given in our previous papers [Rosa et al. 2008], we investigate energy spectra from intermittent MHD turbulent-like stochastic variability patterns with  $\beta = 2$  (weak turbulence) and  $\beta = 5/3$  (strong turbulence). Here the inhomogeneous nature of the decimetric solar radio emission was successfully detected by using the DFA method on the whole SRB time series. From the point of view of plasma physics, the decimetric SFU time series can be interpreted as being the response of an out-of-



**Figure 3.** The time profile of SRB1 (a), SRB2 (b) and SRB3 (c) showing the respective DFA scaling exponents in (d), (e) and (f).

equilibrium process, possibly related to the particle acceleration from a transversal loop-loop interaction, where MHD oscillations can play an important role and a counterpart phenomena as turbulent interaction between electron beams and evaporation shocks can act as a secondary source. In order to check such hybrid mechanism composed by an inhomogeneous decimetric extended source, higher spatial resolution data are required. Once the decimetric solar bursts analyzed here are related to geoeffective events, the microphysics processes as particle acceleration and magnetic reconnection can be addressed in a more general scenario involving the plasma solar-terrestrial environment. Then, in the framework of the solar radio activity, our results strongly suggest the use of the DFA scaling exponent as a computational measure for solar radio burst automatic monitoring system (RBAMS), which has been developed for a real-time Data System Representation [Veronese et al. 2009] in the scope of the Brazilian Space Weather Program.



**Figure 4. Evolution of  $\alpha$  for each SRB before starting the correspondent flare. In each curve is shown a box indicating the window(s) - time interval - where the flare occurs.**

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